Descriptive Statistics Refiesher

MTT pics discussed in these reviews licks are in bold

- 1. Measure of set operations
- 2 Conditional/joint probabilities
- 3 Courtingrules
- 4 Measues of certial tendency and dispersion
- 5 Distributions (including normal and binomia)
- 6 Sampling and estimation
- 7. Hypothesis testing
- 8 Carelation and regression
- 9 Time series forecasting
- 10 Statistical correpts in quality control

"SOCS"

Whenyouandyzeaset of data, remember "SOCS"

Shape—what is the shape of the distribution?

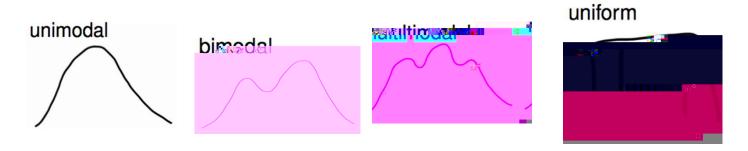
Others—Are there any unusual data values in the distribution?

Center—How can I best describe the typical value or center of the distribution?

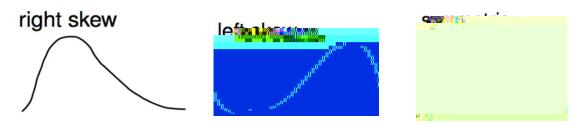
Spread-HowcanIdescribe the variation or dispersion in the data?

Comorlychservedshapes

Modelity.



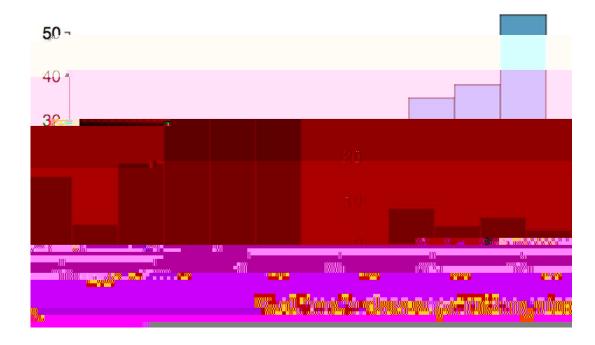
Sewress crymmetry.



Histogram

Commongaphforquatitative data The horizontal axis is an unber ire boken into ranges and the vertical axis is the court or frequency

Stape slevedleft



Otles

Anottierisadatavaluethat appeas extreme relative to the rest of the data

Otlies can often be identified by examining an appropriate graph of the data

Someouties are data entry or data collection en os that can be consected after they are identified. Other outies are natural features of the data

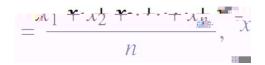
Since outlies impact many calculations, you should impect your data for outlies near the beginning of your analysis

Centercreential tendency

Measures of central tendency the center; armiddle, artypical value of a distribution

Communeasue of certe: meanand median

Mean The sample mean, denoted as x, can be calculated as



wherex, x, ..., x represent the deserved values

Mean

The population mean is also computed the same way but is denoted as µ It is often not possible to calculate µ since population data are rarely available

The sample mean is a sample statistic, and serves as a point estimate of the population mean This estimate may not be perfect, but if the sample is good (representative of the population),

Medan

The median is the value that splits the data in half when ordered in ascending order

If there are an even number of observations, then the median is the average of the two values in the middle

$$0, 1.2.3.4.5 \rightarrow \frac{2+3}{2} = 2.5$$

Since the median is the midpoint of the data, 50% of the values are below it. Hence, it is also the 50th percentile.

Vaiane

The variance is roughly the average squared deviation from the mean Hueis the form la for the sample variance

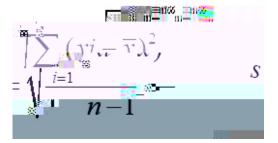
The sample variance is a point estimate of the conesponding population variance. The population variance has a slightly different formula

 $\sum_{i=1}^{N} (x_i - x_i)^2$

Standaddesiation

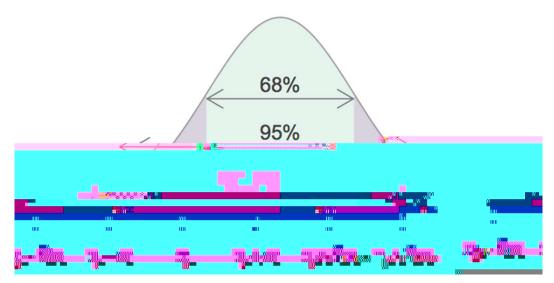
The standard deviation is the squae root of the variance. The unit of measure of the standard deviation is the same as the data. This makes the standard deviation more practical than the variance to use in applications. The SD is interpreted as roughly the average distance between observations in the data set and the mean of the data.

Famla



Empirical rule (cr 6895997 rule)

Inaurimodal, symmetric distribution, about 68% of the values fall within one standard deviation of the mean, about 95% of the values fall within two standard deviations of the mean, and about 997% of the values fall within three standard deviations of the mean



Qatiles

Quitiles are special percentiles that divide a data set into four sections, each containing 25% of the data set.

Q1=first quartile=25th percentile

Q2=secondquartile=50thpercentile

Q8=thidquatile=75thpercentile

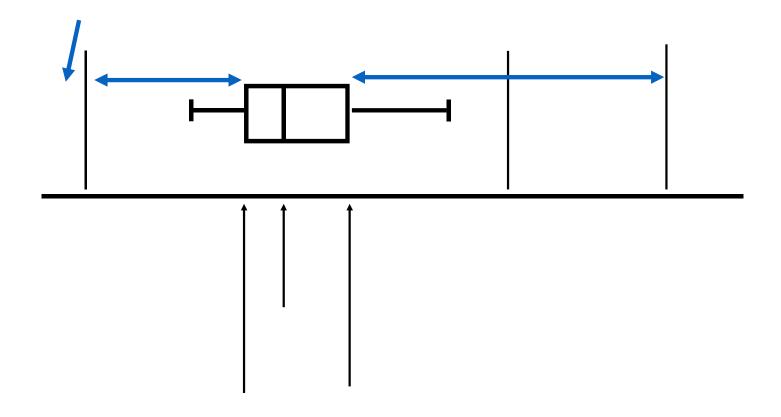


Boxplots

Boxplots (or box and whisterplots) are gaphical displays built from the five number summary. The five number summary consists of the min, QI, median, QB, and max

The boxesterds from Q1 to Q8 A line is drawn inside the box at the value of the median The "whisters" extend to the values of the min and max

Inadition, boxplots are often modified to incorporate outlier detection rules based and stances beyond the quartiles and either 1.5xIQR for potential outliers, or 3xIQR for probable outliers



Zscres

Astandadzedvalue, community called az score, provides a relative measure of the distance and bervation is from the mean, which is independent of the units of measurement.

Subtracting the mean from all data values centers the data set at 0 Dividing all of the centered values by the standard deviation scales the values to a new standard deviation of 1.

The proces it a hiring o

Impatofaties

Officspil the mean

Otlies the value of the range, variance, and standard deviation

(Note measues of variational ways get la ger when outlies are present.)

Otlies also impact other statistics, such as the conelation, coefficients of regression models, etc.

Somestatistics are resistant to the effects of outliers, like the median and IQR

Identifying outliers

There are several communities of thurbforidentifying outliers

- 1) Values above QB+ 1.5xIQR or below Q1 1.5xIQR which are called the "inner fences," are potential outliers
- 2) Values above QB+ 3×IQR or below QI 3×IQR which are called the "outerferces" are probable outliers/extreme values
- 3 Values with z scares above + 3 or below 3 are potential outliers

Choosingappopriatenessues

The mean and standard deviation are the most popular measures of center and variation. If the data is roughly symmetric in shape and contains mode vious outliers, these measures are acceptable.

The median and IQR, which are both resistant to the impact of outliers, should be strongly considered when the data contains outliers or is strongly skewed in shape.

Categorical data

Categorical data is fundamentally different than quantitative/numeric data

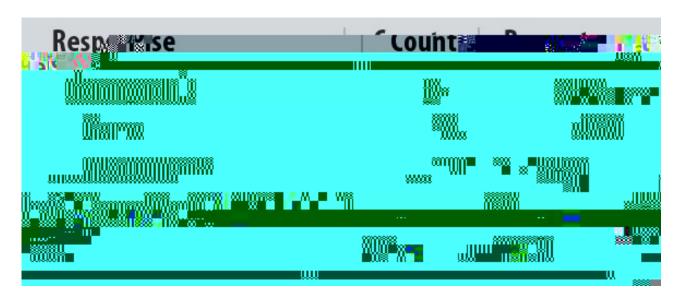
Averages, standarddeviations, and other summary statistics often make no sense for categorical data

Sampleproportion

The sample proportion, denoted by or

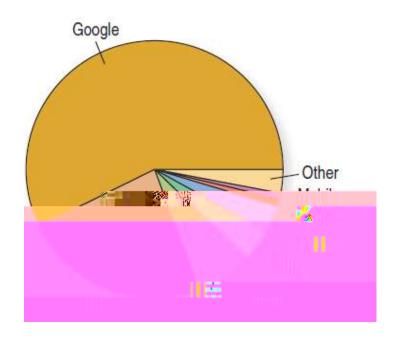
Fiequencydistribution

Afiequency distribution displays the values of a categorical variable and one or more neasures derived from the court of how often each category occurs in the data



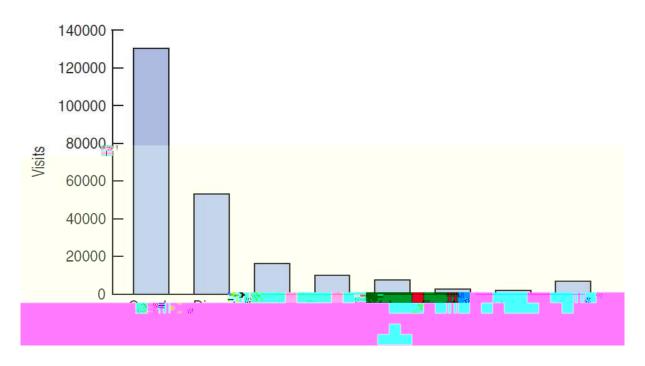
Reduct

Piedrats show the whole group of cases as a circle sliced into pieces with sizes to the first ion of the whole in each category



Barchat

Abardrat displays the distribution of a categorical variable, showing the counts for each category next to each other for easy comparison



Contingencytable

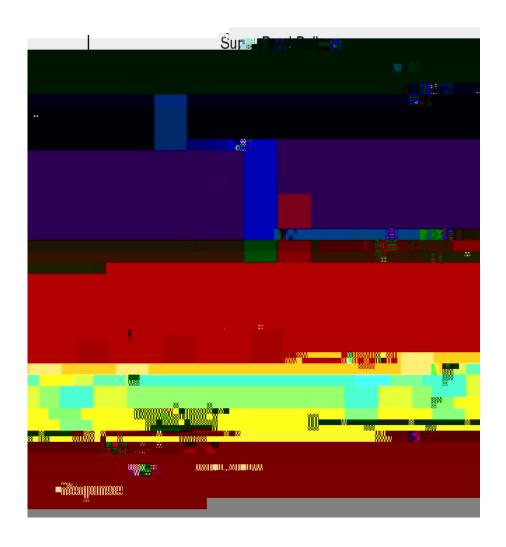
The fiequencies of categorical variables can be summarized and displayed simultaneously using a contingency table (or

aostabilation):



Oberbardats

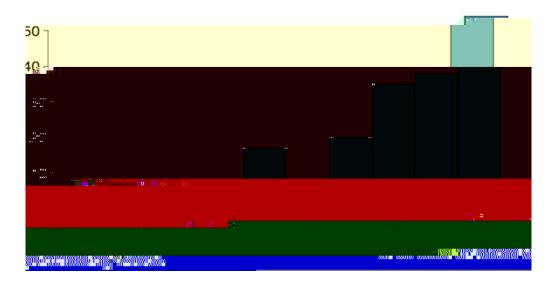
Mneedabaatebardats, such as dustered arstaded bardats can be a cated from contingency tables



A) Which is most likely true for the distribution of "percentage of time actually spert taking notes in class," which is displayed in the

histogan?

- (a) nean> nedan
- (b) nean~ nedan
- (c) mean< median
- (d) impossible totell



- B) Which of these variables do you expect to be uniformly distributed?
- (a) veights of adult females
- (b) salaries of a random sample of people from North Carolina
- (c) house prices
- (d) birthdysof dasanates (day of the month)

D) Acommunity colleges dood board is negotiating a new contract with the college faculty. The distribution of faculty salaries is skewed right by several faculty members who make over \$100,000 per year. If the school board wants to give the community the impression that the faculty are already over paid, should they acker se the mean or median of the faculty salaries?

The school boardshould use the mean to make their argument. The mean will be higher than the median since it will be influenced by the few high salaries

The school boardshould use the necian to nake their argument. The necian will be lower than the nean since the nean is influenced by the few high salaries

The school boardshould use the near to make their argument. The near will be lover than the neckan since the neckan is influenced by the few high scharies

- E) Acompanyadvertises amean lifespan of 1000 hous for a particular type of light bulb. If you were incharge of quality control at the factory would you prefer that the standard deviation of the lifespans for the light bulbs be 5 hous or 50 hous? Why?
 - 50 hous would be preferable since a larger standard deviation indicates a larger average lifespan for the light bulbs
 - 5 hous vould be preferable since a smaller standard deviation indicates note consistency
 - 50 hous would be preferable since a larger standard deviation indicates note consistency
 - 5 hous would be preferable since a smaller standard deviation indicates a longer average life span for the light bulbs

Padicesolution

- A) Which is nost likely true for the distribution of "percentage of time actually spert taking notes inclass," which is displayed in the histogram?
- (c) mean< median

The distribution is slewed to the left and the data values in the left tail pull

Pactice solution

- B) Which of these variables do you expect to be uniformly distributed?
- (d) birthdysof dassnetes (day of the month)
- Of fsomeone's gossamual income has a z some of +23 what can be concluded?

Their income is 23 standard deviations above the mean income

Partices dution

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5housvouldbepreferablesine asmaller standard deviation indicates more consistency.